

CS 110 Computer Architecture Datapath

Instructors: Siting Liu & Chundong Wang

Course website: https://toast-

lab.sist.shanghaitech.edu.cn/courses/CS110@ShanghaiTech/Spring-2024/index.html School of Information Science and Technology (SIST) ShanghaiTech University

2024/4/2

Administratives

- Lab 5 available, please prepare in advance! Lab 6 will also be released before the Qingming holiday.
- HW 3 available, ddl April 9th, start early!
- Proj1.1 ddl approaching, April 8th
- Proj1.2 released soon, ddl April 25th
- Future discussion (teaching center 301) schedule:
 - Friday (April 5th) no discussion (QingMing holiday).
 - April 7th (班) discussion on digital circuit basics by TA Yang Chao.
 - April 8th, mid-term review by Yang Chao.
 - After that, the same content for Friday and the next Monday.
- Labs on Thursday (April 4th) will be checked on Sunday (April 7th), 18:00-19:40. Please contact your TAs if you have further concerns.

Mid-term I

- Midterm I
 - April 11th 8:00 am 10:00 am
 - We start sharp at 8:00 am!
 - Arrive 7:45 am to check-in (three classrooms likely and seat table will be determined on-site)
 - Arrive later then 8:30 am will get 0 mark.
- Contents:
 - Everything till April 9th lecture
- Switch cell phones off!!! (not silent mode)
 - Put them in your bags.
- Bags in the front. On the table: nothing but pen, exam paper, 1 drink, 1 snack, your student ID card and your cheat sheet!

Mid-term I requirements

- You can bring a cheatsheet (handwritten only). 1-page A4, double-sided (2-page for the mid-term II and 3-page for the final). Put it on your desk at exam. Cheatsheet that does not apply to the rules would be taken away.
- <u>Greencard</u> shown on the course website is provided with the exam paper.
- No other electronic devices are allowed!
 - No ear plugs, music, smartwatch, calculator, computer...
- Anybody touching any electronic device will **FAIL** the course!
- Anybody found cheating (copy your neighbors answers, additional material, ...) will **FAIL** the course!









Cheat Sheet

- 1 A4 Cheat Sheet allowed (double sided)
 - Midterm II: 2 pages
 - Final: 3 pages
- Rules:
 - <u>Hand-written</u> <u>not printed/photocopied!</u>
 - Your **<u>name</u>** in pinyin on the top!
 - Cheat Sheets not complying to this rule will be <u>confiscated</u>!

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· Find the extreme values of f on the Boundary of D The largest value from 3, 2, 15 the ABS, MAX, the sourcest is the ABS, MAX in the sourcest is the ABS MAX in the sourcest is the source of the sourcest is the source sourcest is the sour	**************************************					
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Outline

- Useful building blocks
 - ALU design
 - Register file
 - Memory considerations
- Datapath
- Design of the controller

• A classic problem: sequence detection for "010" (non-overlapping)

Input: <u>0 1 0 0 1 0</u> 1 0 1 1 0 Output: 0 0 0 1 0 0 1 0 0 0 0

- Step 1: Draw finite state machine of the desired function (we ignore the initialization)
- Step 2: Define/assign binary numbers to represent the states, the inputs and the outputs
- Step 3: Write down the truth table (enumerate input/previous state (and current state) and their corresponding current state (and output))
- Step 4: Use template and decide the combinational block for state transition and output logic

• A classic problem: sequence detection for "010" (non-overlapping)



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• Step 3: Write down the truth table (enumerate input/previous state (and current state) and their corresponding current state (and output))

















	P	revious	sstate	Currer	nt state	
	input	S[1] _{k-1}	S[0] _{k-1}	S[1] k	S[0] k	output
Detected/1 0 detected/0 (00)	0	0	0	0	1	0
	0	0	1	0	1	0
	0	1	0	1	1	1
	0	1	1	0	1	0
	1	0	0	0	0	0
	1	0	1	1	0	0
	1	1	0	0	0	0
28	1	1	1	0	0	0

Controller & Datapath

• A CPU that support RV32I can have so many states



- Consider the 32 registers alone
 - x0 always 0
 - Each bit in the other registers can be 0 or 1
- Not practical to enumerate all the state transitions
- Top-down design: build small modules and then connect them as needed
- Most digital systems can be divided into datapth and controller
 - Datapath contains data processing and storage
 - Controller controls data flow and state change (still can be modeled as FSM)
- Recall the execution of an instruction
 - Our Goal: Implement a RISC-V processor as a synchronous digital system.
 - Each RV32I instruction can be done within 1 clock cycle (single-cycle CPU).

Controller & Datapath

• A CPU that support RV32I can have so many states



- Datapath
 - Start with basic building blocks
 - Add building blocks to the digital system with added supported instructions
- Controller
 - Can be considered as an FSM

- Our Goal: Implement a RISC-V processor as a synchronous digital system.
- Each RV32I instruction can be done within 1 clock cycle (single-cycle CPU).

Useful building blocks

• An ALU should be able to execute all the arithmetic and logic operations



Useful building blocks

• An ALU should be able to execute all the arithmetic and logic operations



Datapath

Useful Combinational Circuits

• Multiplexer (2-to-1)

• Multiplexer (2ⁿ-to-1)



Control through selection

• 32-bit Multiplexer and logic gates to support some logic instructions



• More layers of multiplexer to select from more inputs

Multiplexer

• n-to-1 multiplexer symbol



Multiplexers used for shifter

- Left shift a single bit -> left shift multiple single bits
- Other shifter designs such as barrel shifter



Useful building blocks

• An ALU should be able to execute all the arithmetic and logic operations



Adder & subtractor

• An adder design



- A smart subtractor design
 - Recall that subtracting a number is equivalent to adding its negative version

A smart subtractor design

A - B = A + (-B) = A + \overline{B} + 1 (mod 2^{N-1})



Useful building blocks

• An ALU should be able to execute all the arithmetic and logic operations



- The register file is the component that contains all the general purpose registers of the microprocessor
- A register file should provide data given the register numbers
- A register file should be able to change the stored value





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How to select one to output? Multiplexer



- The register file is the component that contains all the general purpose registers of the microprocessor
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Recall we have registers that store values



Output

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Useful building blocks-Register file

- The register file is the component that contains all the general purpose registers of the microprocessor
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We have covered PC register previously

- Synchronous digital circuit can have feedback, e.g., iterative accumulator
 - e.g. PC = PC + 4 without considering branch or jump



• Timing diagram



Useful building blocks-Memory

- Memory similar to register file except that the basic cell design is different
- Requires refresh for DRAM



Datapath



Datapath



Datapath for R-type

• We have all the building blocks to execute R-type instructions



Datapath for R-type

• We have all the building blocks to execute R-type instructions



Datapath for I-type arithmetic and logic



Datapath for more types ...

